

SOLVING ALGEBRAIC WORD PROBLEMS

PRAXIS FLASHCARD #76, #364, and #221

CONSECUTIVE NUMBERS

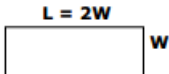
Numbers that follow each other in counting order are called **consecutive**. They can be denoted as $x, x + 1, x + 2, x + 3$, etc. Consecutive odd numbers are $x, x + 2, x + 4$, etc. (assuming x is odd), and consecutive even numbers are also $x, x + 2, x + 4$, etc. (assuming x is even). **Example:** Find three consecutive, even numbers whose sum is 90.

$$\begin{aligned}x + (x + 2) + (x + 4) &= 90 \\3x + 6 &= 90 \\3x &= 84 \\x &= 28 \text{ so the numbers are } \mathbf{28, 30, 32}\end{aligned}$$

PRAXIS FLASHCARD #77

RECTANGULAR AREA & PERIMETER

Problems involving area & perimeter require use of formulas: $P = 2L + 2W$, where P = Perimeter, L = length, W = width. $A = LW$, where A = area. **Example:** The length of a rectangle is twice its width. If the perimeter of the rectangle is 60 in, find its area.


$$\begin{aligned}L &= 2W \text{ so } P = 2(2W) + 2W \\60 &= 4W + 2W \\60 &= 6W \\W &= 10 \text{ and since } L = 2W \\L &= 20 \\ \text{Knowing this, } A &= LW = 20(10) = \mathbf{200 \text{ in}^2}\end{aligned}$$


PRAXIS FLASHCARD #78

TRIANGLES

Problems involving triangles require you to know facts about triangles, such as: Two angles that form a straight line (180°) are supplementary. The sum of the measures of the interior angles of a triangle is 180° .

Example: Find the unknown angle (x):


$$\begin{aligned}x + 90 + (180 - 140) &= 180 \\x + 90 + 40 &= 180 \\x + 130 &= 180 \\x &= \mathbf{50^\circ}\end{aligned}$$

PRAXIS FLASHCARD #79

UNIT CONVERSION

Set up **unit conversion problems** as a proportion. Then cross multiply (Means- Extremes Property) and simplify. (Unit analysis may also be used – see the flashcard on unit analysis.) **Example:** Convert 16 yards to feet. Because there are 3 feet in 1 yard:

yard	1	16
feet	3	??

Cross multiply: $3 \times 16 = \mathbf{48 \text{ feet}}$

PRAXIS FLASHCARD #80

MIXTURES

Problems involving mixtures use $M_1V_1 + M_2V_2 = M_3V_3$, where M is the percentage of each mixture, and V is the volume or amount of each mixture. **Example:** How much of a 16% solution is needed to combine with 34 ml of a 12% solution to make 50 ml of a 15% solution?

$$\begin{aligned}0.16x + 0.12(34) &= 0.15(50) \\16x + 12(34) &= 15(50) \\16x + 408 &= 750 \\16x &= 342 \\x &= \mathbf{21.375 \text{ ml}}\end{aligned}$$

PRAXIS FLASHCARD #81

INVESTMENTS

Problems involving investments require use of the interest formula: $I = Prt$, where I = interest earned, P = principal (original amount), r = annual rate of interest, and t = time in years. **Example:** An investment is made at 5% simple interest for 12 years. It earned \$420 interest. How much was originally invested?

$$\begin{aligned} 420 &= P(.05)(12) \\ 420 &= 0.6P \\ 4200 &= 6P \\ P &= 4200/6 \\ \mathbf{P} &= \mathbf{\$700} \end{aligned}$$

PRAXIS FLASHCARD #82

DISCOUNTS

Problems involving discounts require use of the discount formula: $S = r - rd$, where S is the sale price, r is the retail price, and d is the rate of discount. **Example:** A coat is on sale for \$125. If the coat was discounted 20%, what was the original retail price?

$$\begin{aligned} 125 &= r - (0.2)r \\ 125 &= (0.8)r \\ (\text{multiply both sides by } 10 \text{ to clear decimal}) \\ 1250 &= 8r \\ r &= 1250/8 \\ \mathbf{r} &= \mathbf{\$156.25} \end{aligned}$$

PRAXIS FLASHCARD #83

COMMISSIONS

When we think of **sales commissions**, we often think of car sales. Thus, it is appropriate that the formula for commission is $C = ar$, where C = commission earned, a = amount of sale, and r = commission rate.

Example: Juana sells cars on a 3% commission rate. She just sold a car for \$23,500. What was her commission?

$$\begin{aligned} C &= ar \\ C &= 23500(.03) \\ \mathbf{C} &= \mathbf{\$705} \end{aligned}$$

PRAXIS FLASHCARD #84

DISTANCE--RATE OF SPEED--TIME

The **distance formula** is $D = rt$, where D is the distance traveled, r is the rate of speed, and t is the time.

$$r = \frac{D}{t} \text{ to calculate the rate of speed} \qquad t = \frac{D}{r} \text{ to calculate the time}$$

PRAXIS FLASHCARD #85

UNIFORM MOTION

In problems where you are given data about an object traveling **with** and then **against** a moving object, use a table, and then set the SAME quantities equal to each other & solve. The distance formula is $D = rt$

	D	r	t
Direction One Way			
Opposite Direction			

Example: A boat can travel 12 mi/hr in still water. If the boat can travel 5 mi downstream in the same time it takes to travel 3 mi upstream, what is the rate of the river's current?

	D	r	t=D/r
Direction One Way	5	$12 + c$	$\frac{5}{12 + c}$
Opposite Direction	3	$12 - c$	$\frac{3}{12 - c}$

$$\text{Set } \frac{5}{12 + c} = \frac{3}{12 - c} \text{ and solve for } c.$$